

Calculi for Reasoning About Action and Knowledge

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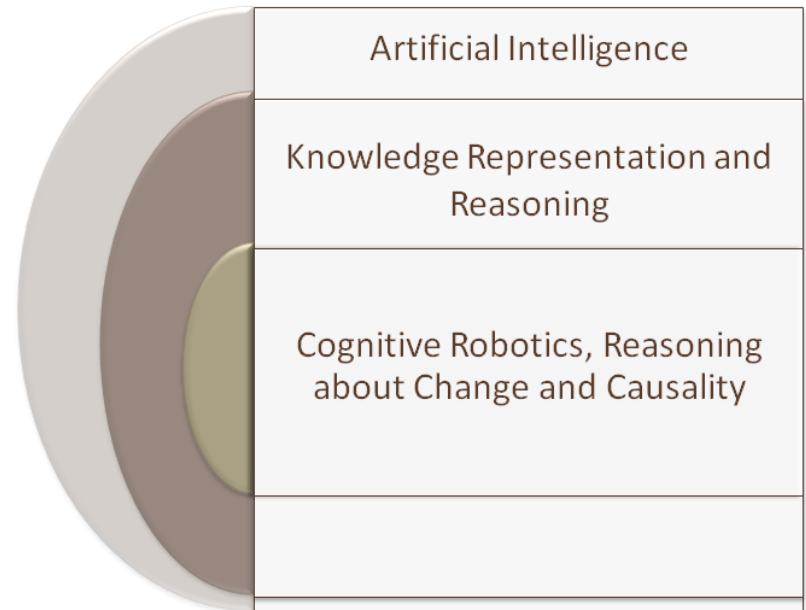
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Outline

- Reasoning about action and change
- Fundamental issues
- Active Research Domains
- Application Domains
- Epilogue

Action Theories – Introduction

- Action theories are logical languages devised to express the *dynamics* of the world
- They aim at “*formally characterizing the relationship between the knowledge, the perception and the action of autonomous agents*” (Levesque, Reiter [17])
- Action theories model (explicitly or implicitly) the general notions of *time, change* and *causality*.
- During the 1990's the attention in action theories revolved around *cognitive robotics*.



Action Theories – Introduction

- Action Theories are formal tools that aim to automate the process of *commonsense reasoning* in dynamically-changing worlds, in order to
 - predict the outcome of a given action sequence
 - explain observations
 - find a situation in which certain goal conditions are met.
- Action theories have much in common with general purpose logics
 - In the general case they are based on *predicate calculus*.
- State transition and plan generation is done by *logical deduction*, rather than by state-space or plan-space search.

Action Theories – Commonsense phenomena

- Related issues
 - Representation
 - Effects of Events and Causal relations
 - Indirect Effects of Events (*Ramification problem*)
 - Context-dependent Effects
 - Non-deterministic Effects
 - Concurrent Events
 - Preconditions
 - Inertia (*Frame problem*)
 - Actions with duration
 - Physical and Triggered events
 - Delayed Effects and Continuous Change
 - Default Reasoning (*Qualification problem*)
 - ...

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Fundamental Issues – The Frame Problem

- Example (definitions of sorts are missing):

$$Happens(?e, ?t) \wedge Initiates(?e, ?f, ?t) \Rightarrow HoldsAt(?f, ?t+1) \quad (4.0)$$

$$Initiates(TurnOn(?x), On(?x), ?t) \quad (4.1)$$

$$\neg HoldsAt(On(Light1), 0) \quad (4.2)$$

$$\neg HoldsAt(On(Light2), 0) \quad (4.3)$$

$$Happens(TurnOn(Light2), 0) \quad (4.4)$$

- Ok about *Light2*, but what can we say about *Light1*??

Fundamental Issues – The Frame Problem

- The *frame problem* refers to the task of
 - expressing the effects of a world changing action
 - without having to explicitly specify all the aspects that are not affected by this action.
- Different solutions have been proposed
- A popular one is the axiomatization of the commonsense *Law of Inertia*:
 - “*things tend to persist unless affected by some event*”.

Fundamental Issues – Ramification Problem

- An action can cause a series of direct effects, but can also have dramatic *side-effects*.
- The problem of representing and reasoning about the indirect effects of events is known as the *ramification problem*.
- A multitude of solutions have been proposed, but still this is an open and very challenging issue.

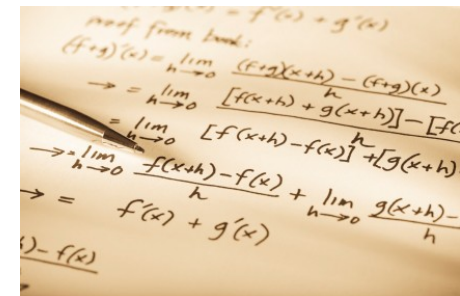


Fundamental Issues – Qualification Problem

- Whenever we intend to execute some plan we know that many *things may go wrong*, i.e.,
 - in order to drive to the university the car must have gas,
 - its engine must not be broken,
 - its tailpipe must not be blocked by a potato or other object,
 - the roads must not be blocked
 -
- If we *lack evidence to the contrary*, commonsense instructs to proceed assuming that none of the potential problematic cases holds.
- It is impossible to list all contingencies! This is the so-called *qualification problem*:
 - “an agent needs not consider unexpected qualifications for an action, unless there is evidence to justify their existence”.

Fundamental Issues – Challenging research topics

- Incorporating a *uniform solution* for all three problems is a challenging task
- For instance, while many existing approaches to the frame problem are monotonic, the qualification problem inherently requires a non-monotonic solution
- Additionally, ramifications in real world are *too complex* (delayed effects, unknown parameters) and require a combination of different reasoning types, e.g., temporal reasoning.



Handwritten mathematical proof for the limit of a sum of functions:

$$\begin{aligned} \text{proof from book:} \\ (f+g)'(x) &= \lim_{h \rightarrow 0} \frac{(f+g)(x+h) - (f+g)(x)}{h} \\ &= \lim_{h \rightarrow 0} \frac{[f(x+h) + g(x+h)] - [f(x) + g(x)]}{h} \\ &= \lim_{h \rightarrow 0} \frac{[f(x+h) - f(x)] + [g(x+h) - g(x)]}{h} \\ &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} + \lim_{h \rightarrow 0} \frac{g(x+h) - g(x)}{h} \\ &= f'(x) + g'(x) \end{aligned}$$

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Prominent Calculi – Languages and implementations

- Situation Calculus [1,2,3]
 - First-order language with some second-order features
 - Defines disjoint *sorts* for actions, fluents, situations (history of actions)
 - *Idea*: Reachable states are definable in terms of the actions required to reach them
 - *Branching* time structure (all actions are hypothetical)
 - Solutions to most problems in the area (not unified solutions)
 - High-level Robot Programming Languages: Golog, IndiGolog etc
- Event Calculus
- Action Languages A , C , $C+$, K [6,7]

Prominent Calculi – Languages and implementations

- Situation Calculus [1,2,3]
- Event Calculus [4,5]
 - First-order *non-monotonic* language, augmented with an explicit representation of *time*
 - *Idea*: Representation of causal and narrative information
 - *Linear* time structure, discrete or continuous time (actual actions)
 - Supports the modeling of a wide variety of phenomena for commonsense reasoning
 - SAT- and ASP-based solvers
- Action Languages *A*, *C*, *C+*, *K* [6,7]

Prominent Calculi – Languages and implementations

- Situation Calculus [1,2,3]
- Event Calculus [4,5]
- Action Languages A , C , $C+$, K [6,7]
 - Define independent *semantics* to distinguish between a claim that a formula is true and the stronger claim that *there is a cause for it to be true*
 - Concise syntax, parts of natural language
 - Developed originally as a means to *translate* the different action languages in a common formalism for correctness assessment; but significantly extended since.
 - Close relation with *Answer Set Programming*: Efficient ASP solvers, Causal Calculator (CCALC) etc

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The AI Landscape – Dynamic Worlds

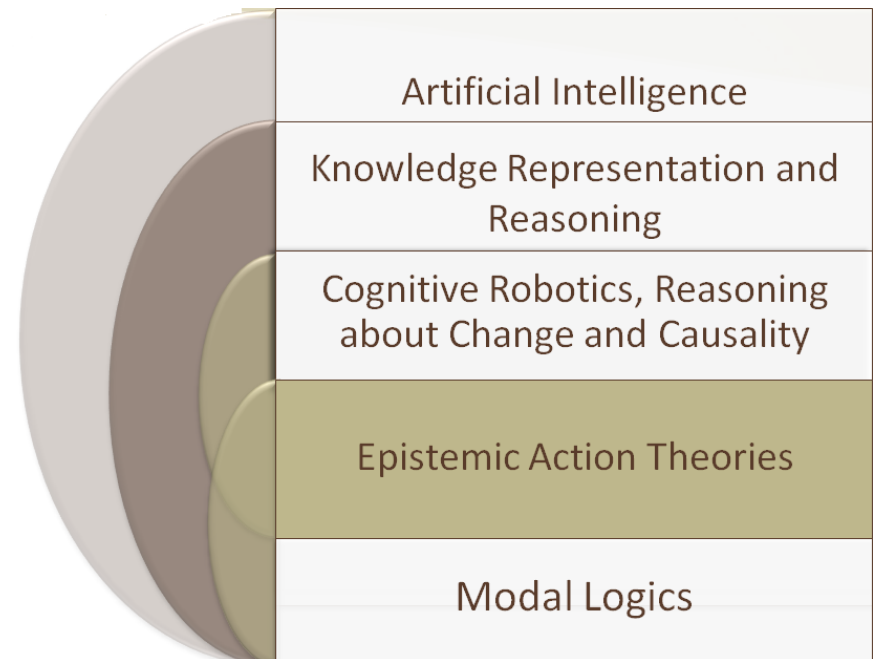
- Commonsense Reasoning in the presence of incomplete knowledge



Epistemic Action Theories

- Epistemic (modal) logic: *An agent is said to **know a fact** if this is true in all possible worlds.*

$$\begin{array}{c}
 \hline
 t=0 \\
 \hline
 s_1^0: \langle \neg f, f' \rangle \\
 s_2^0: \langle \neg f, \neg f' \rangle \\
 \hline
 \hline
 \text{Knows}(\neg f), \neg \text{Kw}(f')
 \end{array}$$

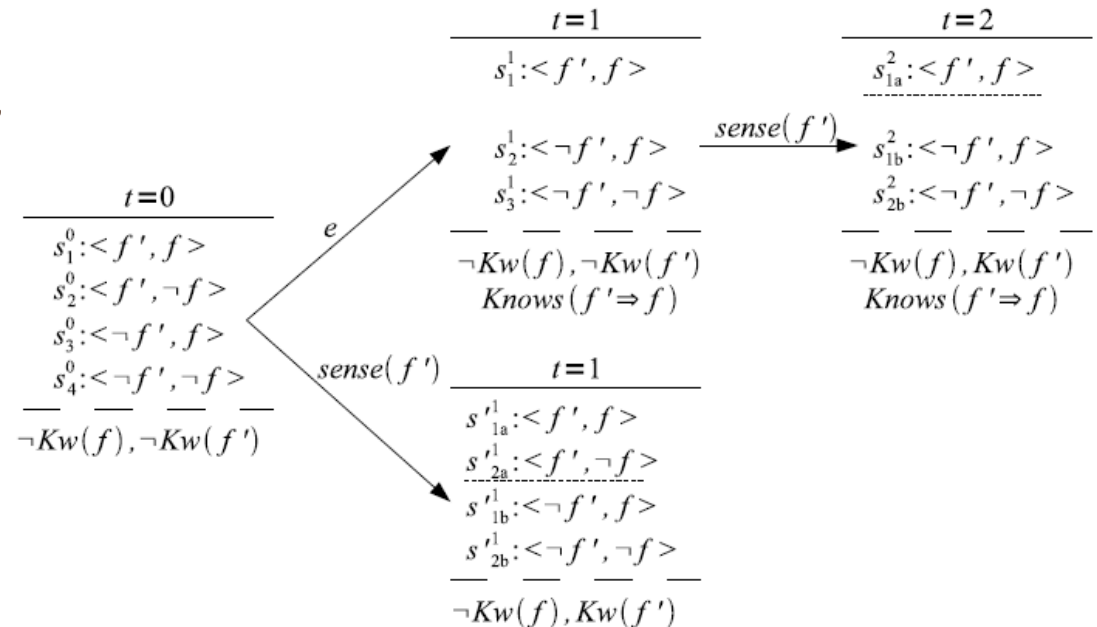


Epistemic Action Theories – Relevant Issues

- How to reason about actions in **partially observable worlds**
 - What do we know about the (direct/indirect) effects of an action, when some preconditions are unknown?
 - When to perform **sensing** and how knowledge should be updated
 - affects our previous knowledge about preconditions
 - affects our assumptions about exogenous actions
 - Build **epistemically feasible plans** (the goal is always *known* to be achievable)
 - What do we know about the effects of **natural/triggered events** when it is not certain whether the state of the world justifies their occurrence?
 - Etc...

Epistemic Action Theories – Possible worlds semantics

- Epistemic action theories [8] are *very expressive* and have been extended in a multitude of way:
 - concurrent actions,
 - belief,
 - future/past knowledge,
 - potentially triggered events,
 - etc...



- But they are *computationally intensive*.

Epistemic Action Theories – Alternative Approaches

- Defining knowledge using the accessibility relation introduces serious *complexity issues*
- ... and there is always the logical omniscience problem.
- Alternate approaches, aiming at tractability, either
 - *restrict expressiveness* (do not support knowledge about disjunctions, restrict the domain) or
 - *sacrifice completeness* with respect to possible worlds semantics.

Epistemic Action Theories – Alternative Approaches & DECKT

- At FORTH we have been working on the Discrete time Event Calculus Knowledge Theory (DECKT) [9]
- DECKT uses a *deduction-oriented* rather than a possible-worlds based model of knowledge.
- It adopts a meta-approach to transform a non-epistemic domain description into an epistemic axiomatization



Epistemic Action Theories – Alternative Approaches & DECKT

- At the core is an established *translation* of the standard possible worlds approach of epistemic reasoning into a form of epistemic implication rules
- When appropriately restricted, it is shown to be sound and complete with respect to possible worlds-based theories
- And more appropriate for *practical implementations* in terms of computational complexity and efficiency in implementing the cognitive skills for agents.



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Multi-Agent Reasoning – Active Research Domains

- “After agent A distracts agent B and takes her key, B will not know that A has the key, and will believe that A does not have it; A knows that B does not know that A has the key”. [10]
- Observability of actions
 - Some actions are *broadcast*; others may be *private*; their effects may be *partially observable* etc
- Nested epistemic notions
 - Reasoning about the epistemic implications of actions on *the mental state of other agents* is instrumental for decision making

Multi-Agent Reasoning – Active Research Domains

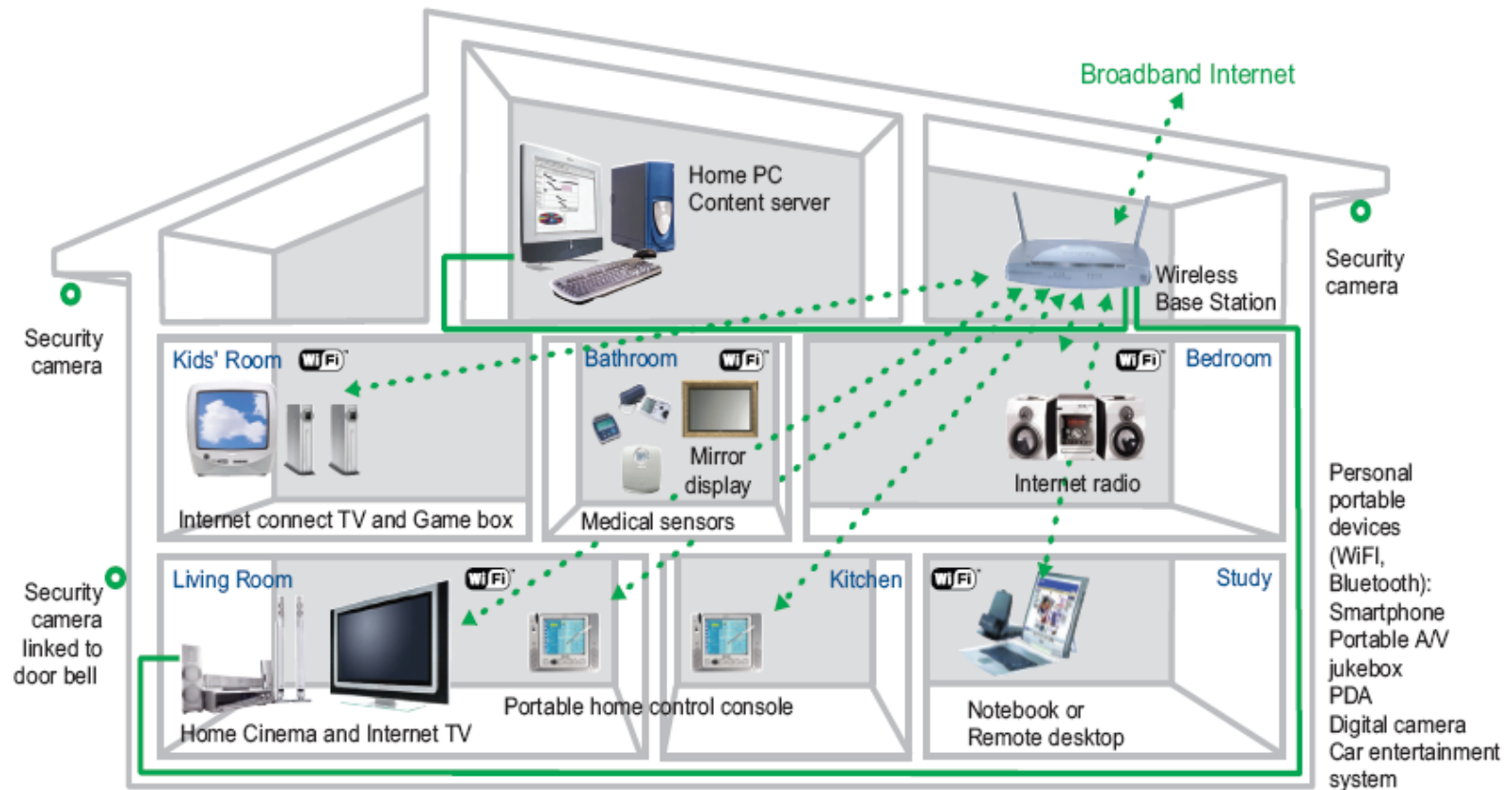
- Group-level epistemic modalities
 - Group knowledge, common knowledge, common goals
- Prospective/Retrospective/Counterfactual Reasoning
 - deliberating about the ramifications of a potential action *in the future* or about how current observations can be explained *in the past*
 - resembles the type of commonsense reasoning humans extensively perform to decide their actions.

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 - Cognitive Robotics
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Ambient Intelligence

- Sensor-rich collaborative environments
- Temporal constraints are ubiquitous



Ambient Intelligence – and AI

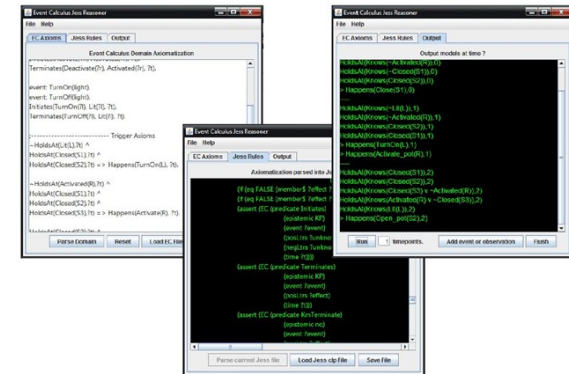
- Aml follows on from work in *Artificial Intelligence*.
- AI has a decisive role to play:
 - representation of contextual knowledge,
 - context inference,
 - collaboration of devices to achieve common objectives,
 - planning in dynamic domains,
 - commonsense reasoning



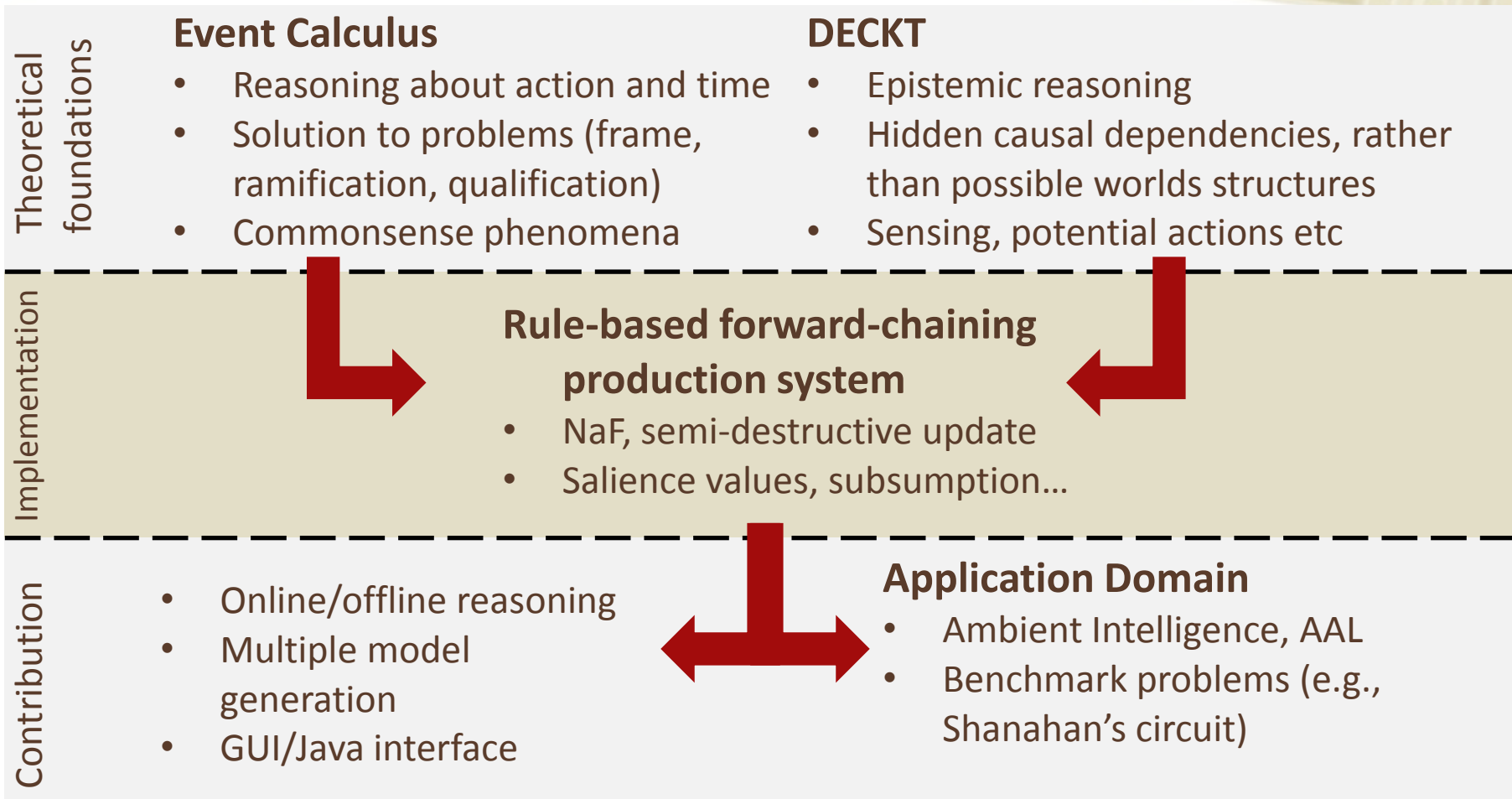
- Low level
Context

Ambient Intelligence – Related Research at FORTH

- At FORTH we implemented a *Semantic Web-based framework* for Aml domains that enables the gathering and dissemination of contextual knowledge..
- ..as well as the design of a *reasoner* [12] for causal, epistemic and temporal reasoning.
- The reasoner translates Event Calculus axiomatizations into production rules for execution of runtime reasoning tasks.



Ambient Intelligence – Event Calculus Rule-based Reasoner



Outline

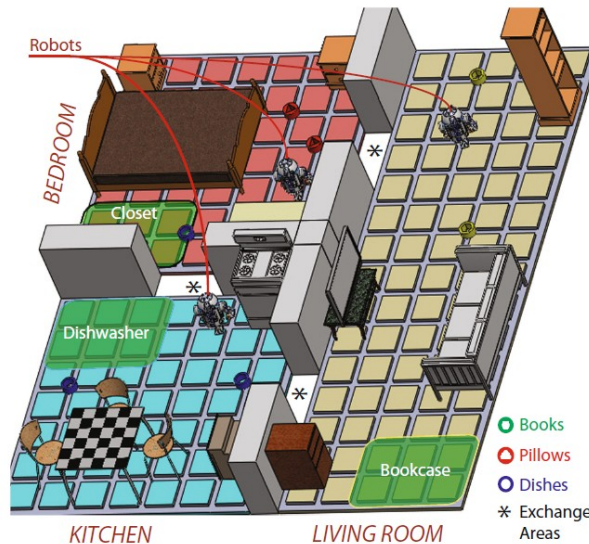
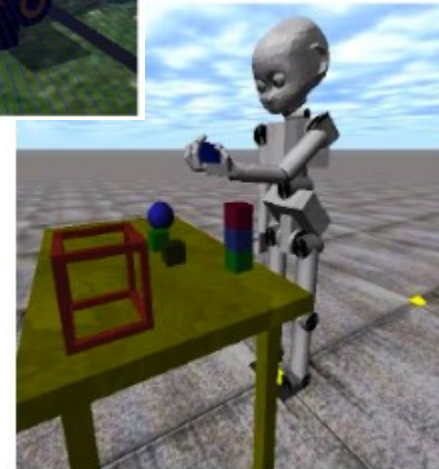
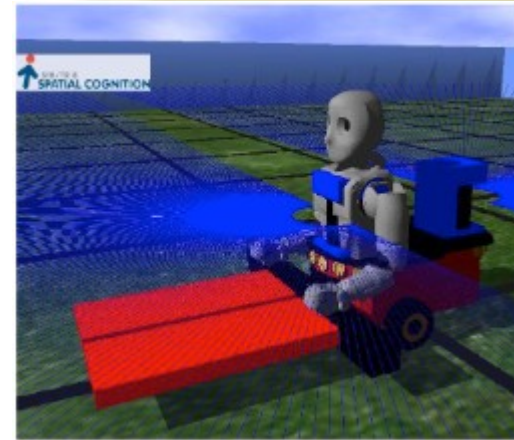
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Cognitive Robotics Today

- Attention is focusing on bringing closer *traditional* with *cognitive robotics*.
- *Bilateral interaction* between causal reasoning and motion planning
- Embedding of *commonsense knowledge*

Cognitive Robotics Today

- Housekeeping robots, simulation platforms and others
- Action theories are now translated and implemented in the new logic-based problem solving paradigm of *Answer Set Programming* (ASP) [18]
- ASP solvers outperform SAT- or Prolog-based reasoners



Other Application Domains

- Complex Event Detection
 - Emergency rescue operations of the Fire Department of Dortmund [13]
 - City Transportation Management [14]
 - Recognition of human activities from video streams [15]
- Web Service Composition
- Commitment Tracking
- and others...



Outline

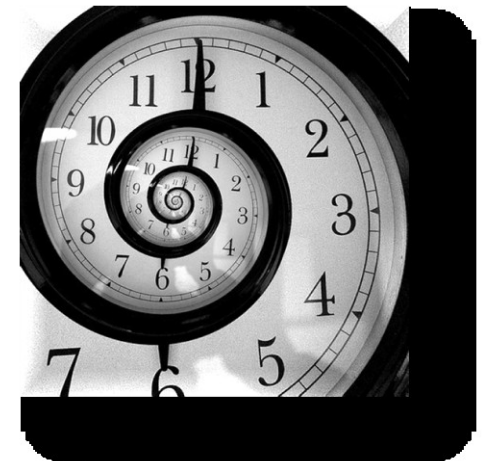
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Epilogue

- Action Theories constitute an active research domain with
 - open theoretical research questions and
 - clear applied orientation
 - (sometimes even a bit beyond:

Leora Morgenstern, “*A Formal Theory of Time Travel*” [16])

- Research in Action Theories both feeds and takes advantage of the progress in logic formalisms
 - Non-monotonic logics: default logic, circumscription, answer set programming



The end

Thank you!



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